## **CLAIM AMENDMENTS**

## **Claim Amendment Summary**

## Claims pending

• Before this Amendment: Claims 1-37.

• After this Amendment: Claims 1, 3-5, and 7-37

Non-Elected, Canceled, or Withdrawn claims: 2, 6

Amended claims: 1, 9, 20, 35

New claims: None

#### Claims:

1. (Currently Amended) A computer-readable medium having computer-executable instructions that, when executed by the system, direct a computer to perform performs a method comprising:

obtaining a message M;

defining a vector v to be  $v_1,...,v_n$  based upon a predefined first hashing function of the message message M:

calculating a private key a in accordance with this equation  $\alpha = \sum_{i=1}^{r} v_i \alpha_i \mod m$ , where m is an order of torsion points;

producing a signature S in accordance with this equation:  $S = aH_2(M)$ , where  $H_2(M)$  is a predefined second hashing function of the message message M, wherein the predefined first hashing function differs from the predefined second hashing function and wherein the signature S is represented by a number of bits:

truncating a specific number of bits off of signature S;

after the truncating, indicating results a message-and-signature pair (M, S) based, at least in part, on the obtaining, defining, calculating, or producing.

# 2. (Cancelled)

**3. (Original)** A medium as recited in claim 1, wherein the results of the indicating comprises a message-and-signature pair  $(M, \mu S)$  and the method further comprises calculating  $\mu = H_3(BK, M)$ , where BK is key and  $H_3(BK, M)$  maps M into an integer within a defined range.

**4. (Original)** A medium as recited in claim 1, wherein the  $a_i$  are scaling factors for n discrete logs of  $\alpha_i P, ..., \alpha_n P$  base P, where n is a positive integer, P is a point on an elliptic curve and a public key.

**5.** (**Original**) A medium as recited in claim 1, wherein

 $q_i$  are scaling factors for n discrete logs of  $\alpha_i P, ..., \alpha_n P$  base P, where n is a positive integer, wherein P is a point on an elliptic curve;

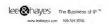
a point P is of order m and where  $e_m(P,Q): E[m] \times E[m] \to GF(q)^*$  denotes a Tate or Weil or Squared Tate or Squared Weil Pairing, where  $\alpha_1 P, ..., \alpha_n P = Q, ..., Q_n$  and where q is a prime power.

## 6. (Cancelled)

- (Original) A medium as recited in claim 1, wherein the first hashing function produces values in {±1}.
  - **8.** (**Original**) A computing device comprising:

an output device:

a medium as recited in claim 1.



**9. (Currently Amended)** A computer-readable medium having computer-executable instructions that, when executed by the system, direct a computer to perform performs a method comprising:

choosing n discrete logs of  $\alpha_1 P, ..., \alpha_n P$  base P, where n is a positive integer, P is a point on an elliptic curve and a public key, and  $a_i$  is a scaling factor and a private key;

indicating results of the choosing;

forging one or more short digital ciphers based upon the indicated results of the choosing.

- **10. (Original)** A medium as recited in claim 9, wherein a point P is of order m and where  $e_m(P,Q): E[m] \times E[m] \to GF(q)^*$  denotes a Tate or Weil or Squared Tate or Squared Weil Pairing, where  $\alpha_1 P, ..., \alpha_n P = Q_1, ..., Q_n$  and where q is a prime power.
- **11. (Original)** A medium as recited in claim 9 further comprising generating a digital signature based upon a message M and a,
  - 12. (Original) A computing device comprising:

an output device;

a medium as recited in claim 9.

**13. (Original)** A method facilitating the production of a digital signature, the method comprising:

obtaining a message M;

defining a vector v to be  $v_1,...,v_n$  based upon a predefined first hashing function of the message;

calculating a private key a in accordance with this equation  $\alpha = \sum_{i=1}^n v_i \alpha_i \mod m$ ;

producing a signature S in accordance with this equation:  $S = aH_2(M)$ , where  $H_2(M)$  is a predefined second hashing function of the message;

indicating results based, at least in part, on the obtaining, defining, calculating, or producing.

- **14. (Original)** A method as recited in claim 13 wherein the results of the indicating comprises a message-and-signature pair (*M, S*).
- **15. (Original)** A method as recited in claim 13, wherein the results of the indicating comprises a message-and-signature pair  $(M, \mu S)$  and the method further comprises calculating  $\mu = H_3(BK, M)$ , where BK is key and  $H_3(BK, M)$  maps M into an integer within a defined range.
- **16.** (**Original**) A method as recited in claim 13, wherein the  $a_i$  are scaling factors for n discrete logs of  $\alpha_i P, ..., \alpha_n P$  base P, where n is a positive integer, P is a point on an elliptic curve and a public key.



**17. (Original)** A method as recited in claim 13, wherein

 $\alpha_i$  are scaling factors for n discrete logs of  $\alpha_1 P, ..., \alpha_n P$  base P, where n is

a positive integer, P is a point on an elliptic curve;

a point P is of order m and where  $e_m(P,Q): E[m] \times E[m] \to GF(q)^*$  denotes a

Tate or Weil or Squared Tate or Squared Weil Pairing, where  $\alpha_1 P, \dots, \alpha_n P =$ 

 $Q_1,...,Q_n$  and where q is a prime power.

18. (Original) A method as recited in claim 13, wherein the signature

 $\ensuremath{\mathcal{S}}$  is represented by a number of bits, wherein the method further comprises

truncating a specific number of bits off of S before the indicating.

19. (Original) A method as recited in claim 13, wherein the first

hashing function produces values in  $\{\pm 1\}$ .

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**20.** (Currently Amended) A computer-readable medium having computer-executable instructions that, when executed by the system, direct a computer to perform performs a method comprising:

obtaining an input message-and-signature pair (M, S);

defining a vector v to be  $v_1,...,v_n$  based upon a predefined first hashing function of the message;

calculating a point Q on an elliptic curve in accordance with this equation:  $Q = \sum_{i=1}^n v_i Q_i$ ;

comparing pairing outputs of a pair (P, S) and a pair  $(Q, H_2(M))$ , where  $H_2(M)$  is a predefined second hashing function of M and P is a point on the elliptic curve;

indicating results of the comparing.

**21. (Original)** A medium as recited in claim 20 further comprising verifying the input message-and-signature pair (M, S) when the indicated results of the comparing is a match.

## 22. (Original) A medium as recited in claim 20, wherein:

the point P being a point on an elliptic curve and of order m and where  $e_m(P,Q)\colon E[m]\times E[m]\to GF(q)^*$  denotes a Tate or Weil or Squared Tate or Squared Weil Pairing, where  $\alpha_1P,...,\alpha_nP=Q_1,...,Q_n$  and where q is a prime power;

the  $a_i$  being scaling factors for n discrete logs of  $\alpha_i P,...,\alpha_n P$  base P, where n is a positive integer.



**23. (Original)** A medium as recited in claim 20, wherein the method further comprises, when the indicated results of the comparing is not a match, modifying the vector  $\nu$  relative to its previous definition and repeating the defining, calculating, and comparing.

**24. (Original)** A medium as recited in claim 20, wherein the method further comprises:

when the indicated results of the comparing is not indicate a match, modifying the vector  $\nu$  relative to its previous definition;

repeating the defining, calculating, and comparing;

if the indicated results of the comparing still does not a match, then repeating the modifying and the repeating of the defining, calculating, and comparing until the indicated results do match.

**25. (Original)** A medium as recited in claim 20, wherein the method further comprises when the indicated results of the comparing is not a match, repeating the defining, calculating, and comparing with the defining being based upon a predefined third hashing function of the message.

**26. (Original)** A medium as recited in claim 20, wherein the signature S is represented by a number of bits, wherein the method further comprises padding S with a specific number of bits before the defining.

27. (Original) A computing device comprising:

an output device;

a medium as recited in claim 20.

**28. (Original)** A method facilitating the verification of a digital signature, the method comprising:

obtaining an input message-and-signature pair (M, S);

defining a vector v to be  $v_1,...,v_n$  based upon a predefined first hashing function of the message;

calculating a point Q on an elliptic curve in accordance with this equation:  $Q=\sum_{i=1}^n v_iQ_i$ ;

comparing pairing outputs of a pair (P, S) and a pair  $(Q, H_2(M))$ , where  $H_2(M)$  is a predefined second hashing function of M and P is a point on the elliptic curve;

indicating results of the comparing.

**29. (Original)** A method as recited in claim 28 further comprising verifying the input message-and-signature pair (M, S) when the indicated results of the comparing is a match.

**30.** (Original) A method as recited in claim 28, wherein

the point P being a point on an elliptic curve and of order m and where  $e_{-}(P,O): E[m] \times E[m] \to GF(q)^{+}$  denotes a Tate or Weil or Squared Tate or Squared

Weil Pairing, where  $\alpha_i P, ..., \alpha_n P = Q_i, ..., Q_n$  and where q is a prime power;

the  $a_i$  being scaling factors for n discrete logs of  $\alpha_i P, ..., \alpha_n P$  base P, where

n is a positive integer.

31. (Original) A method as recited in claim 28 further comprising,

when the indicated results of the comparing is not a match, modifying the vector

 $\nu$  relative to its previous definition and repeating the defining, calculating, and

comparing.

**32.** (Original) A method as recited in claim 28 further comprising:

when the indicated results of the comparing is not a match, modifying the

vector  $\nu$  relative to its previous definition;

repeating the defining, calculating, and comparing;

if the indicated results of the comparing still does not a match, then

repeating the modifying and the repeating of the defining, calculating, and

comparing until the indicated results do match.

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- **33. (Original)** A method as recited in claim 28 further comprising when the indicated results of the comparing is not a match, repeating the defining, calculating, and comparing with the defining being based upon a predefined third hashing function of the message.
- **34. (Original)** A method as recited in claim 28, wherein the signature *S* is represented by a number of bits, wherein the method further comprises padding *S* with a specific number of bits before the defining.
- **35. (Currently Amended)** A computer-readable medium having computer-executable instructions that, when executed by the system, direct a computer to perform performs a method comprising:

obtaining an input message-and-signature pair (M, S');

defining a vector v to be  $v_1,...,v_n$  based upon a predefined first hashing function of the message;

calculating a point Q on an elliptic curve in accordance with this equation:  $Q = \sum_{i=1}^n v_i Q_i$ ;

comparing pairing outputs of a pair (P, S) and a pair  $(Q, H_2(M))^{\mu}$ , where  $H_2(M)$  is a predefined second hashing function of M and P is a point on the elliptic curve and  $\mu$  is an integer in a defined range;

indicating results of the comparing.

**36. (Original)** A medium as recited in claim 35 further comprising verifying the input message-and-signature pair  $(\mathcal{N}, S)$  when the indicated results of the comparing is a match.

**37.** (Original) A computing device comprising:

an output device;

a medium as recited in claim 35.